

9 10/10/16 10:10 AM

13/10/16 10:10 AM 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

$O(h)$

$\log(h)$

11/10/16 10:10 AM

$O(h)$

$O(h)$

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

$O(h)$

$O(h \log h)$

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

$O(h)$

$O(h + k \log h)$

$O(h \log h)$

11/10/16 10:10 AM

$O(h \log h)$

$O(h \log h)$

11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

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11/10/16 10:10 AM

11/10/16 10:10 AM

11/10/16 10:10 AM

$\psi \sim \lambda$

~~1032~~
1063

$$h = |v|$$

h

h

$$m = |E| \leq n^2 - n$$

1

12 ϕ ENRON

+ insert

8250

107 1/2-07 1981

$$n \log n + n \cdot n$$

10/5/20

10. רבסר - שר
11. מ"ל"ה - שר
12. שר
13. שר
14. שר
15. שר
16. שר
17. שר
18. שר
19. שר
20. שר

11/10 ~ 11/13 15:10 ~ 15:40 15:50 ~ 16:20

decrease in α (15%)

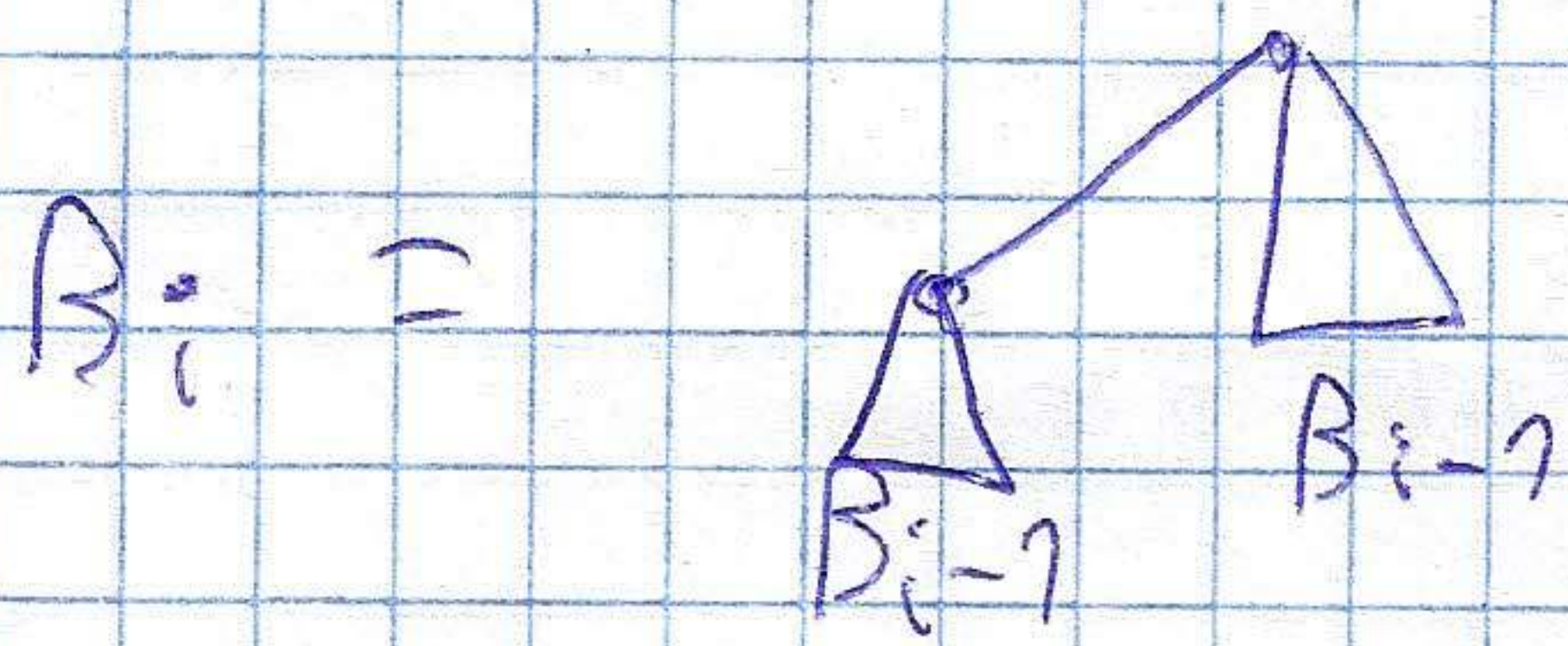
1081 ~~1~~, 1st Nov ~ right

15/5/10 18751 0197 8 8011

$$O(n \log n + m \cdot \log n)$$

$m = O(n^2)$'s, $m \log n$ (c), (d), (e) $\log n$

מכונה נדון

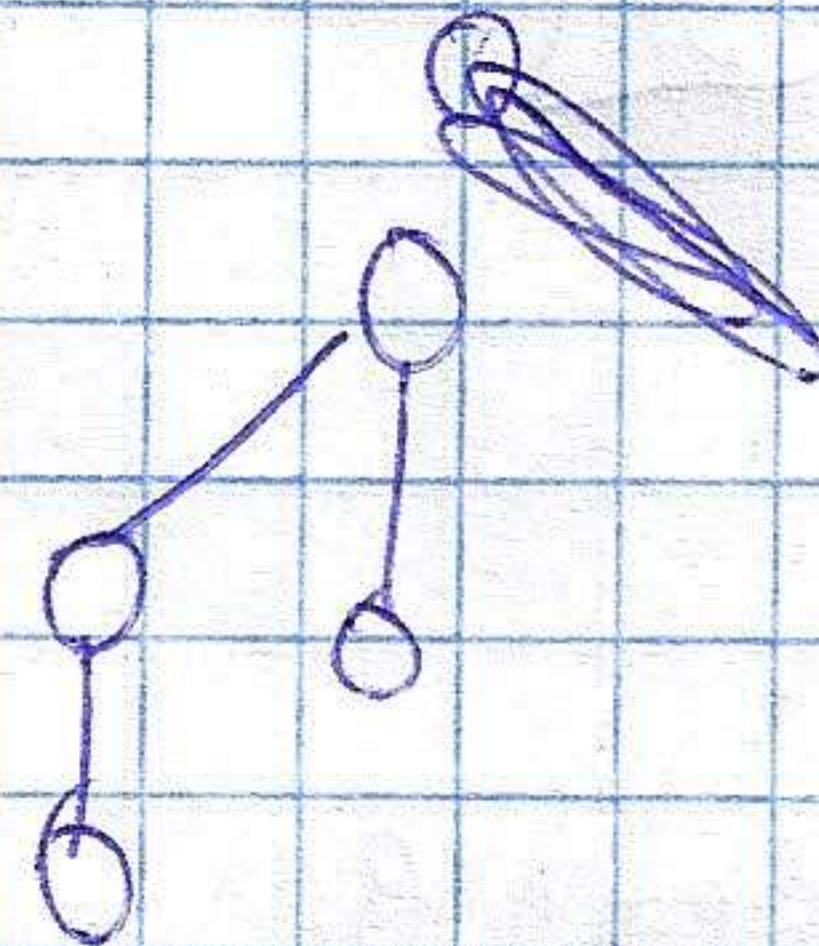


$B_0 = 0$

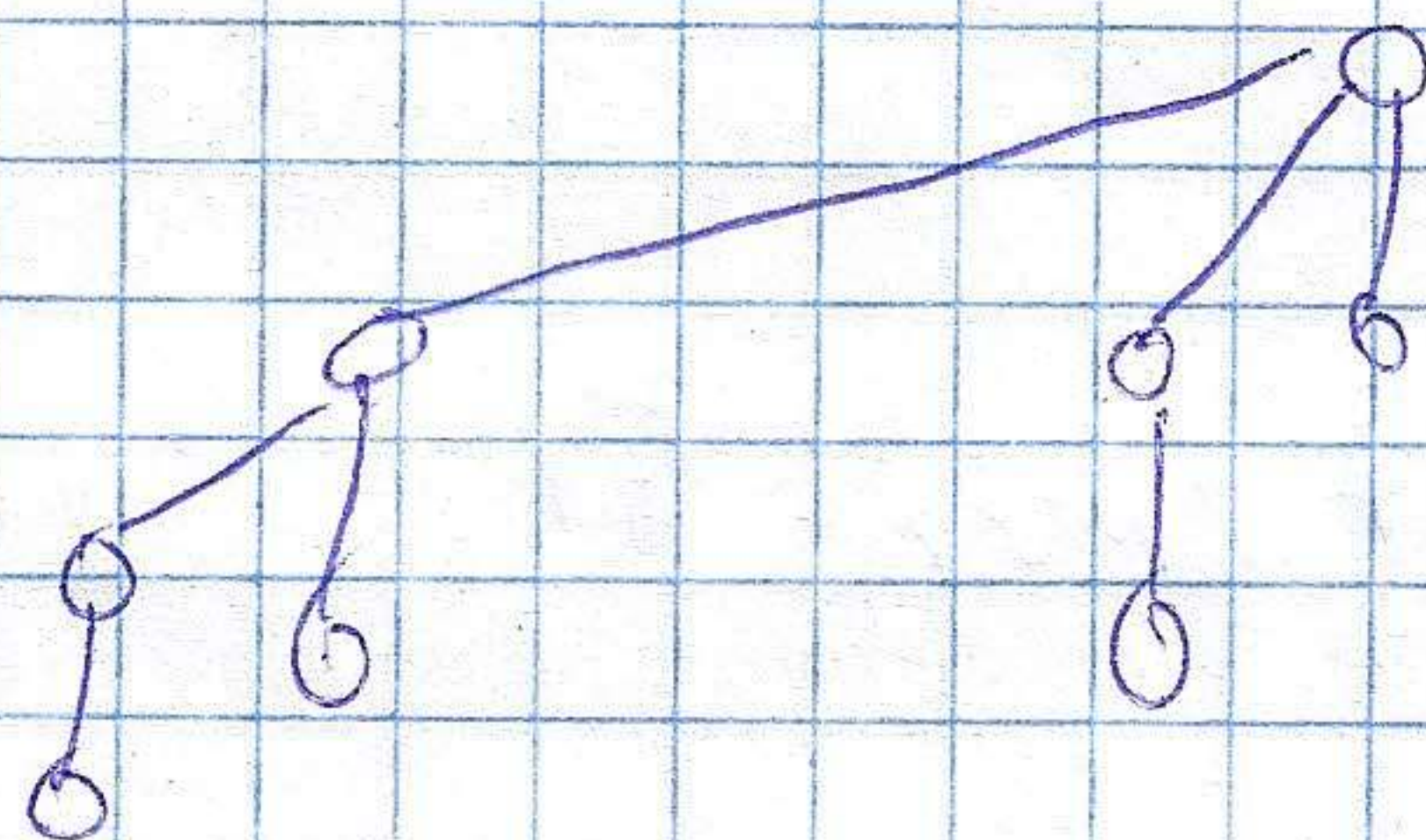
$B_1 =$



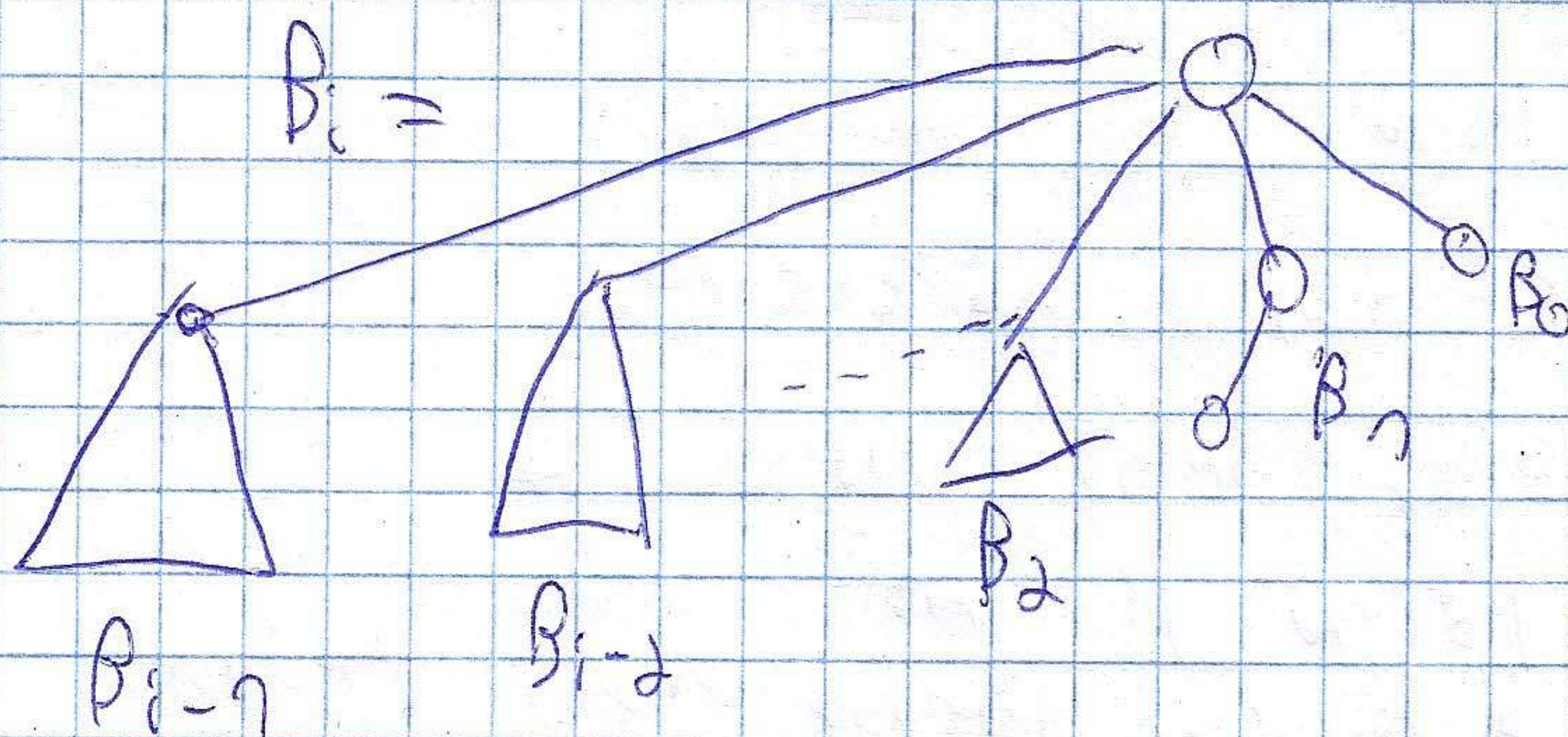
$B_2 =$



הנהגה של B_i היא שכל B_{i-1} הוא עצמו
 כלומר B_i הוא B_{i-1} ו- B_{i-1} הוא B_{i-1}



הנהגה

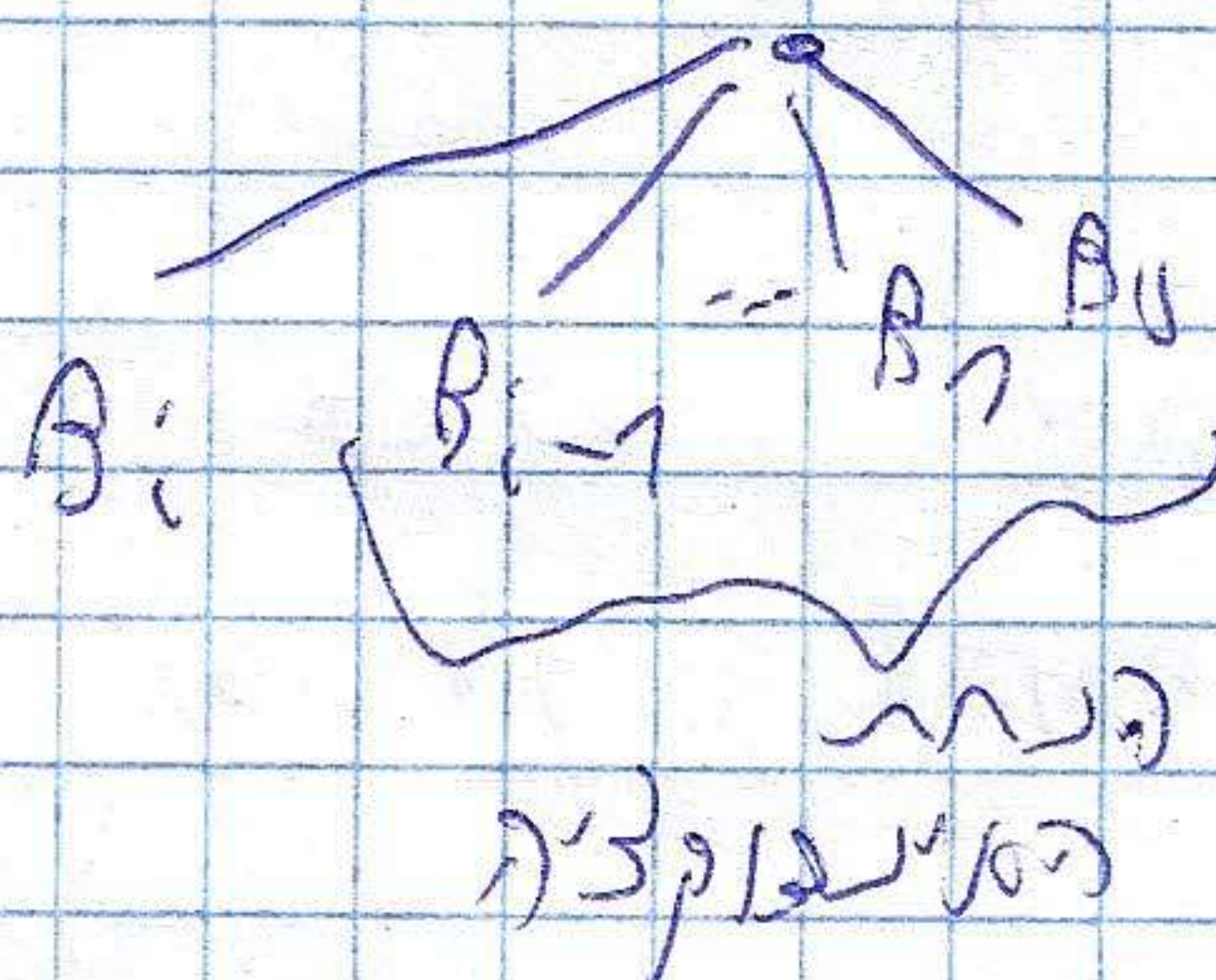
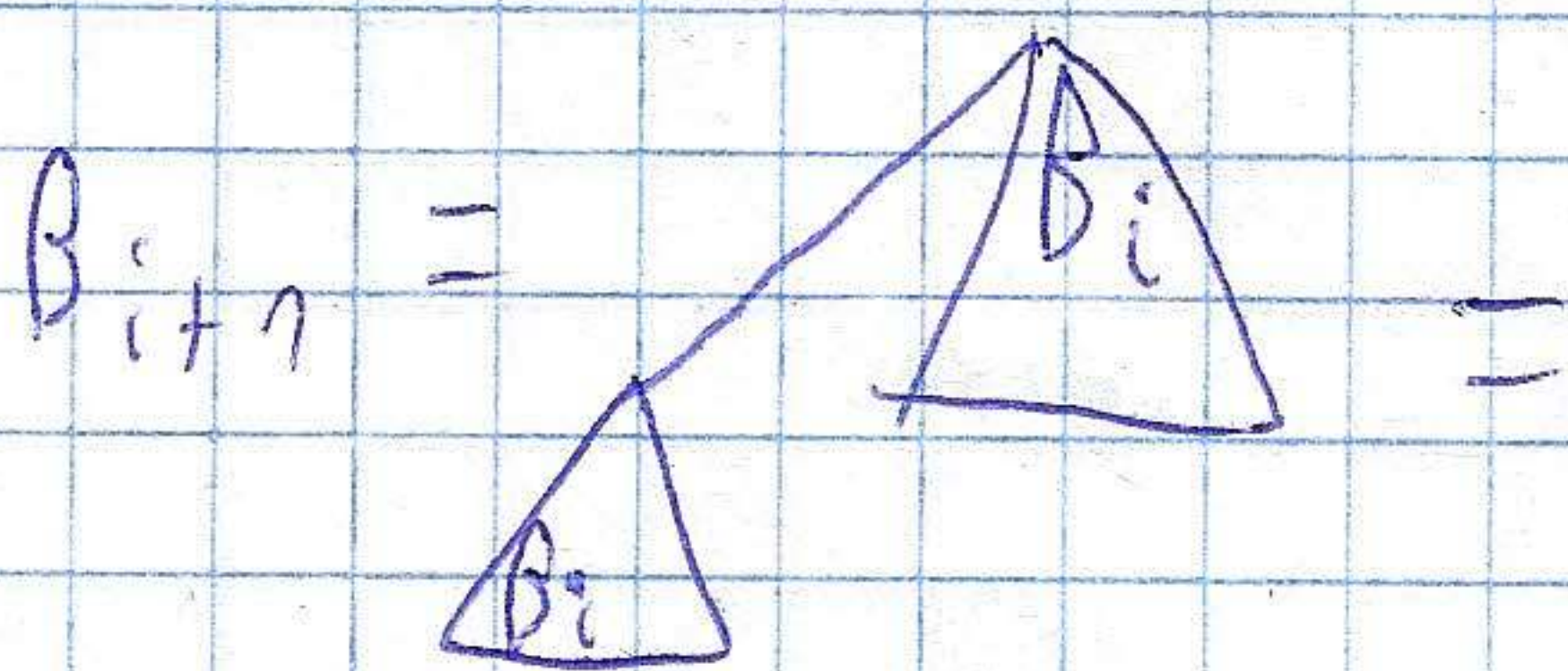


הנהגה של B_i היא שכל B_{i-1} הוא עצמו

$B_i =$ נקודה נקודה

הנהגה

של



$|B_{k+1}| = \left| \begin{array}{c} \triangle B_{1c} \\ \triangle B_k \end{array} \right| \stackrel{1,3,3,1}{=} 2 |B_{1c}| \quad |B_{1c}| = 2^k$

$$\text{depth } B_{1+n} = \text{depth}(B_1) + n$$

1. $\frac{1}{2} \log h$
 2. $\frac{1}{2} \log h$
 3. $\frac{1}{2} \log h$
 4. $\frac{1}{2} \log h$
 5. $\frac{1}{2} \log h$
 6. $\frac{1}{2} \log h$
 7. $\frac{1}{2} \log h$
 8. $\frac{1}{2} \log h$
 9. $\frac{1}{2} \log h$
 10. $\frac{1}{2} \log h$

150 down 3200 2/1/20 108 eie eie

138 W JG) 100
doubly linked list
7
6
5

1. 10/3/88 2. 11/1/88 3. 11/1/88 4. 11/1/88 5. 11/1/88 6. 11/1/88 7. 11/1/88 8. 11/1/88 9. 11/1/88 10. 11/1/88

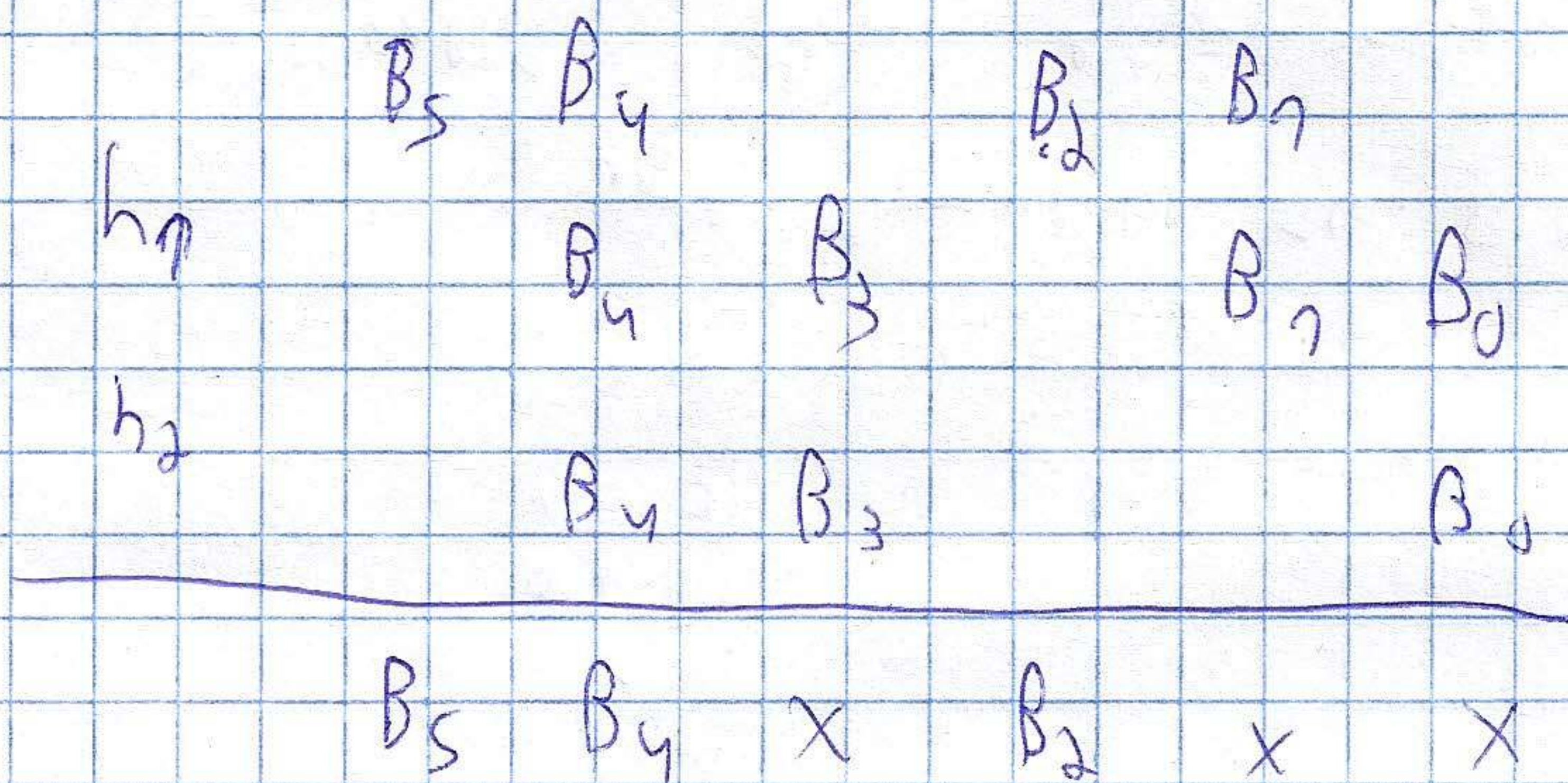
30 million zur Seite Linking

16000 530000000 1000000000

Wiss

essen

Meldung



30 million 1000000000

1000000000 1000000000

15000 1000000000 1000000000 1000000000

$2^k = |B_k|$

1000000000 1000000000 1000000000

$O(1)$ 1000000000 1000000000 find min

1000000000 1000000000 1000000000 Insert x

$O(\log)$

del min

1000000000 1000000000 1000000000

$O(\log)$ meld 1000000000 1000000000

$O(\log)$ 1000000000 1000000000

1000000000 1000000000 1000000000

Dijkstra 1000000000 1000000000 1000000000

1000000000 1000000000 1000000000

1000000000

1000000000 1000000000 1000000000

$O(\log)$

increases by 1

decreases by 1 (x, h, A)

number of nodes in the tree is 2^h

$\log(h)$

~~for all~~

cost of $\log(h)$ is $O(h \log(h))$

total cost of all nodes is $O(h \log(h))$

0 0 0

0 0 1

0 1 0

0 1 1

1 0 0

1 0 1

...

← cost of node is $O(h)$

total cost of all nodes is $O(h \log(h))$

Increment of $\log(h)$

cost of node is $O(h)$

total cost is $O(h \log(h))$

total cost of all nodes is $O(h \log(h))$

total cost of all nodes is $O(h \log(h))$

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total cost of all nodes is $O(h \log(h))$

Amortized $O(1)$

total cost is $O(h \log(h))$

total cost of all nodes is $O(h \log(h))$

total cost of all nodes is $O(h \log(h))$

Lazy melds

do union and find

with union and find

delete min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

del-min /% 50

Amortized = (# links + max rank) - (# links - max - rank)

link /% 50

Array setup

every link removes tree

del-min /% 50

רשימה

Find min $O(1)$ W.C.

Merge $O(1)$ W.C.

Insert $O(1)$ W.C.

מבנה נתון

למה זה?

המבנה הזה הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

delete min Amortized $O(\log)$

הוא מבנה פיל

Decrease key $O(\log)$

Amortized $O(1)$

הוא מבנה פיל

Decrease key

הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

הוא מבנה פיל

$\log h$
 Rank of the tree = degree of the root
 Successive linking
 Delete min
 Insert

Rank of the tree = degree of the root

Successive linking
 Delete min

Insert

Insert

Cascading cuts for decrease key

Node

Node

Node

Node

Node

Node

Node

$O(1)$

Node

Node

Node

$O(1)$
 $O(\log h)$

Cascading cuts
 delete

for non decreasing

work - min - max

decrease a key

no / no

is it possible to find a way to

add a new element to the array

delete min

for decrease key

Insert

decrease n

change the array

log